



# ML in traditional HPC simulations

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# What is Machine Learning/ AI?

## Artificial Intelligence:

Mimicking the intelligence or behavioural pattern of humans or any other living entity.

## Machine Learning:

A technique by which a computer can "learn" from data, without using a complex set of different rules. This approach is mainly based on training a model from datasets.

## Deep Learning:

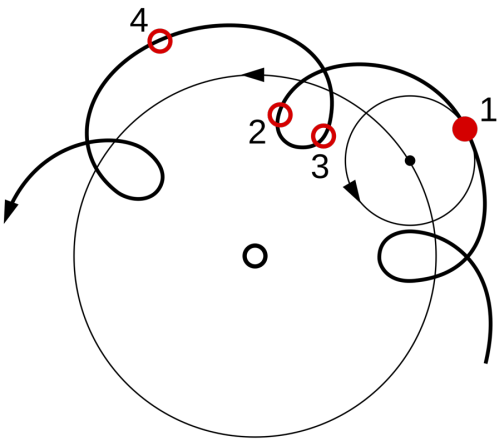
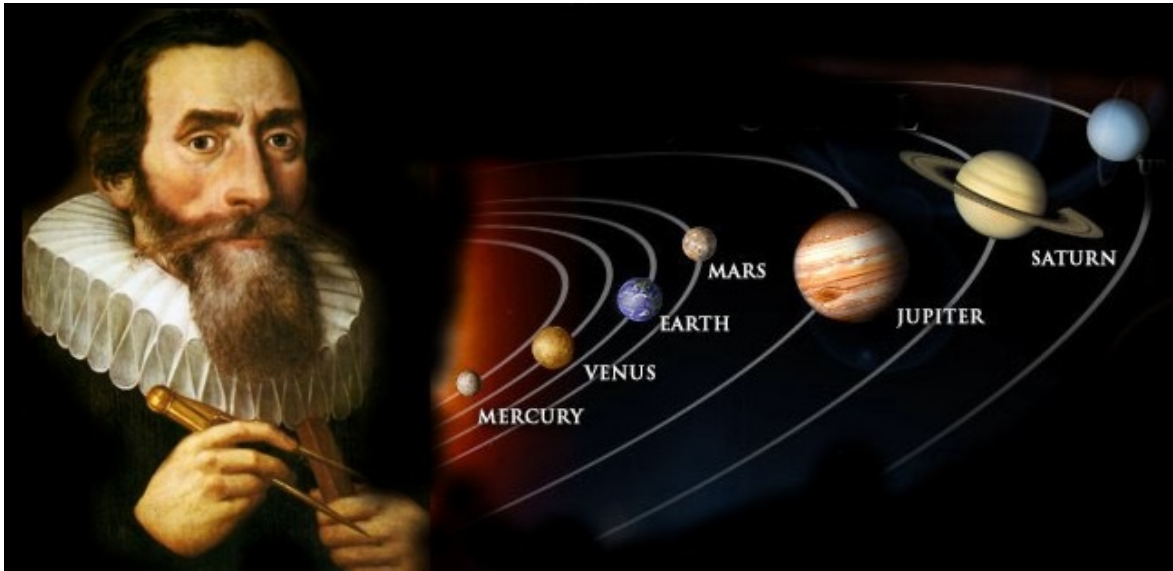
A technique to perform machine learning inspired by our brain's own network of neurons.



AlphaGo competing against legendary Go player Lee Sedol

# Learning from Data

Understanding optimal coordinates in data



Heliocentrism

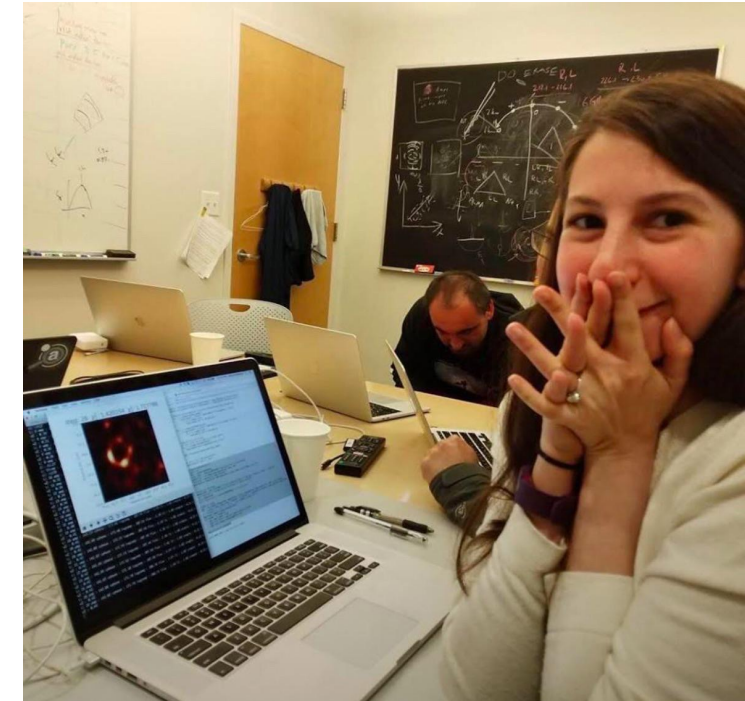
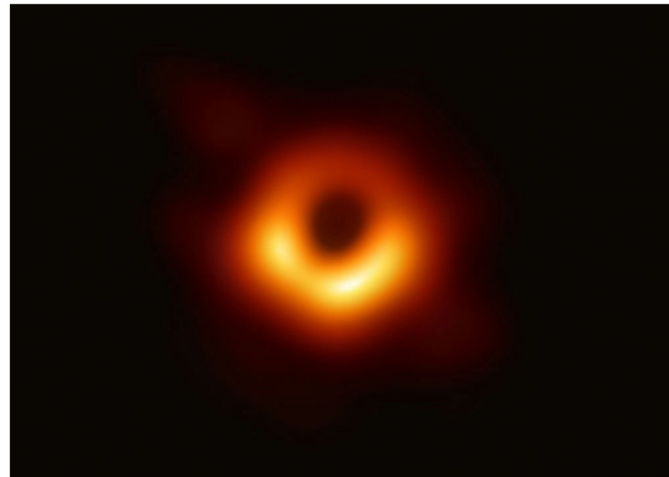
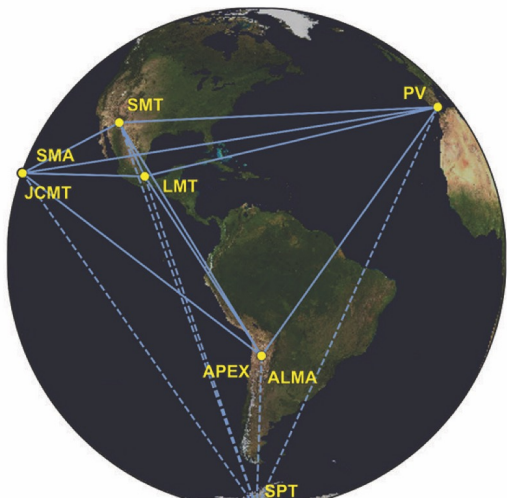
Geocentrism



# Big Data Requires Automated Analysis

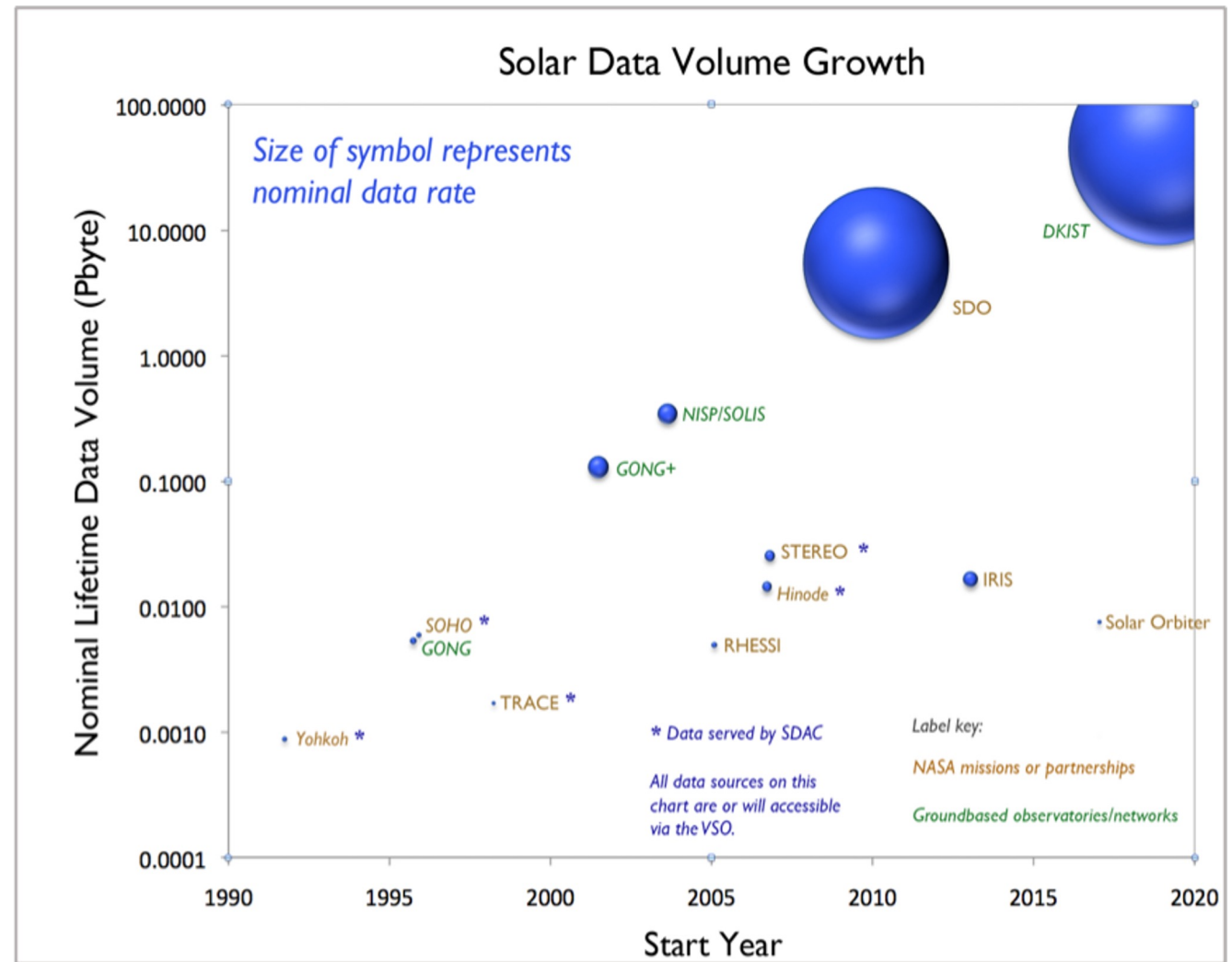
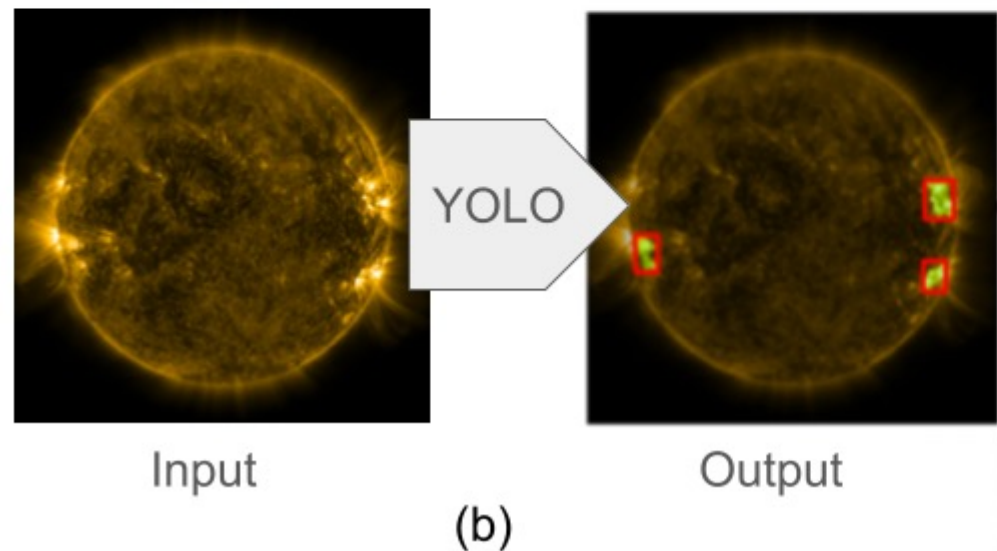
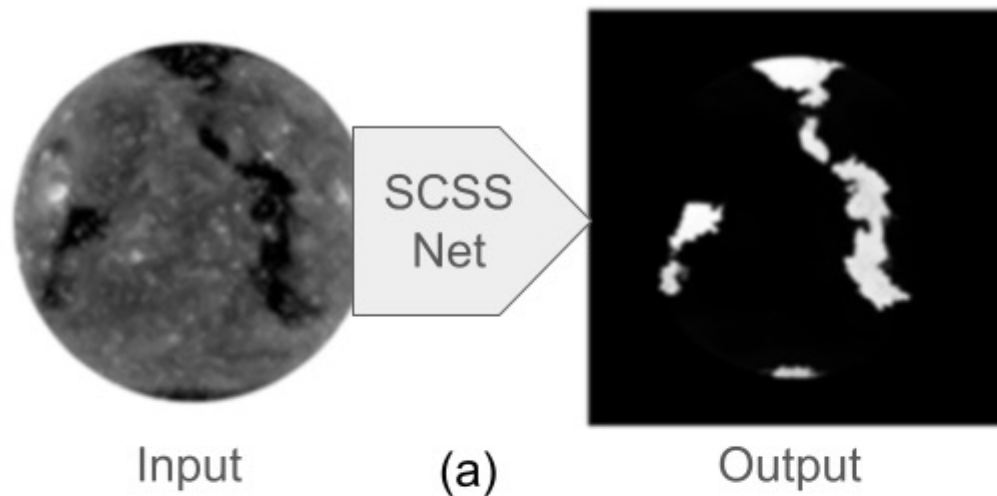
In the last century, you could publish your observation data as a part of your manuscript and analyze them using pen and paper.

- Recent projects might generate Petabytes of data that needs to shipped across the globe.

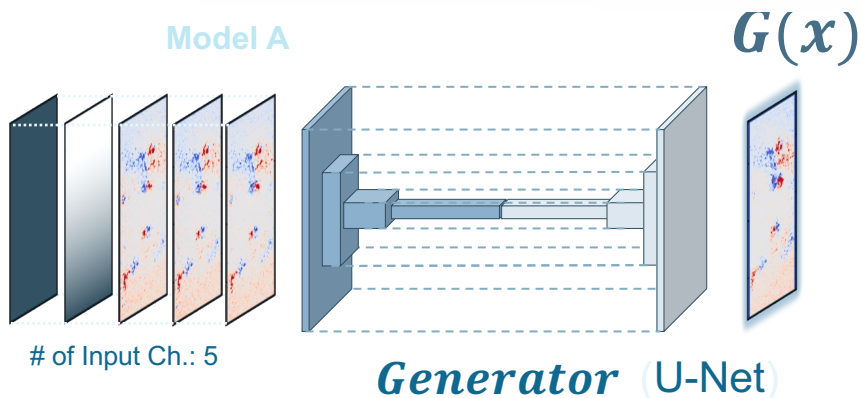
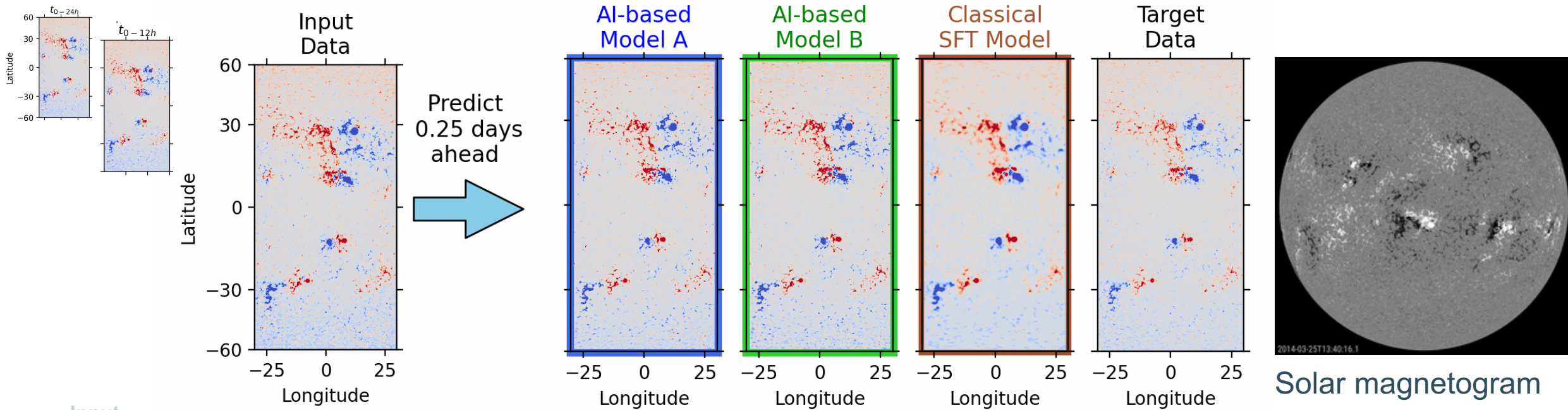


**CHIRP (Continuous High-resolution Image Reconstruction using Patch priors)** is a Bayesian algorithm used to perform a deconvolution on images created in radio astronomy. The acronym was coined by lead author Katherine L. Bouman in 2016

# ML Applications in science: Detection of events



# Machine learning in magnetogram prediction

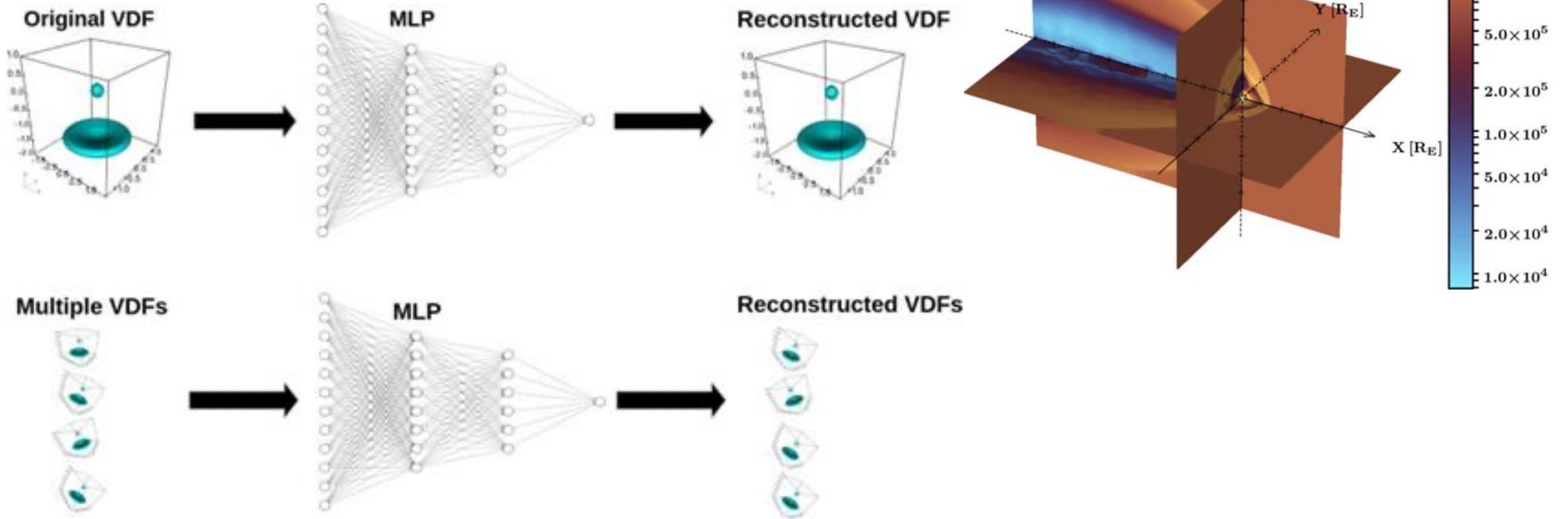


Surface Flux Transport Model:

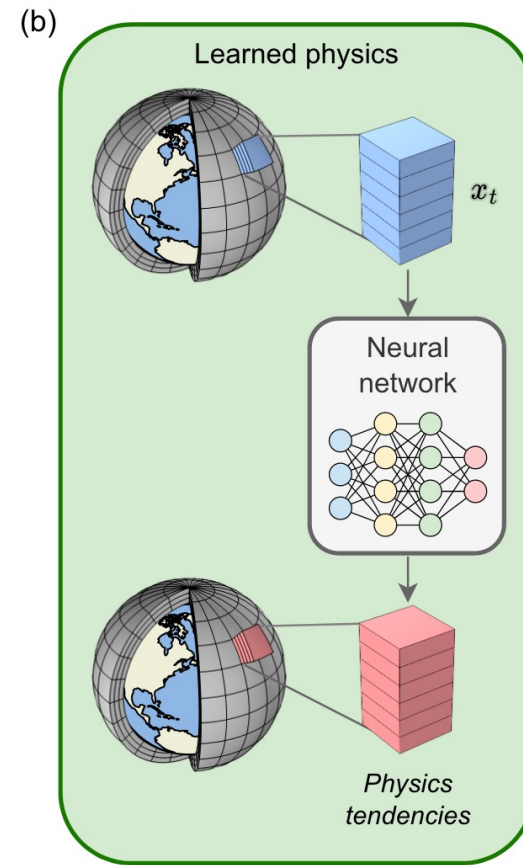
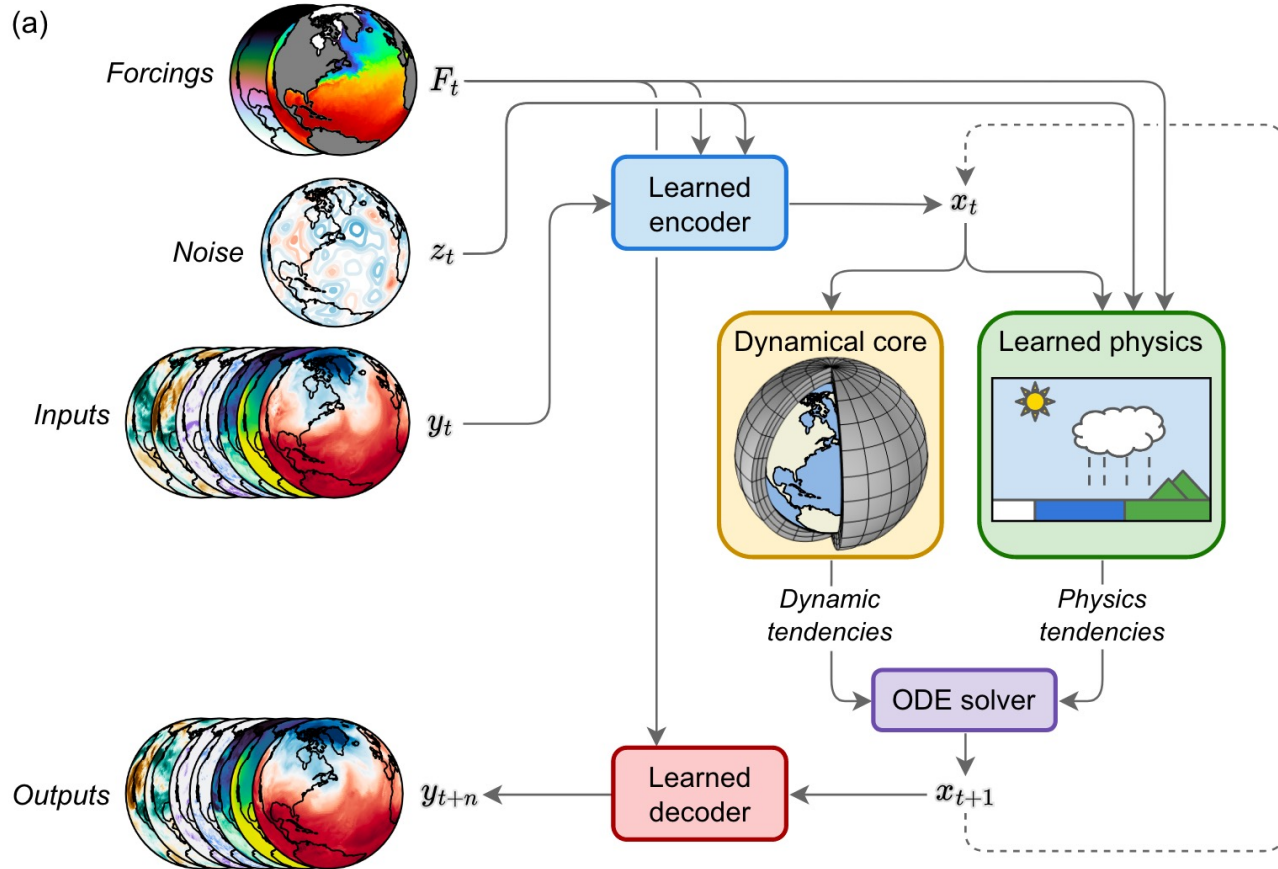
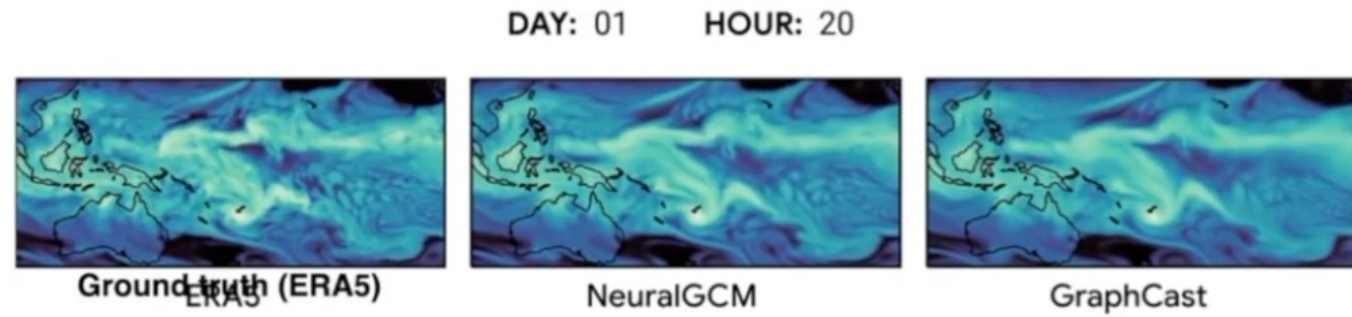
$$\frac{\partial B_r}{\partial t} + \nabla_h \cdot (\mathbf{u}_h B_r) = \eta \nabla_h^2 B_r + S,$$

# Smart checkpointing: compressing saved sims

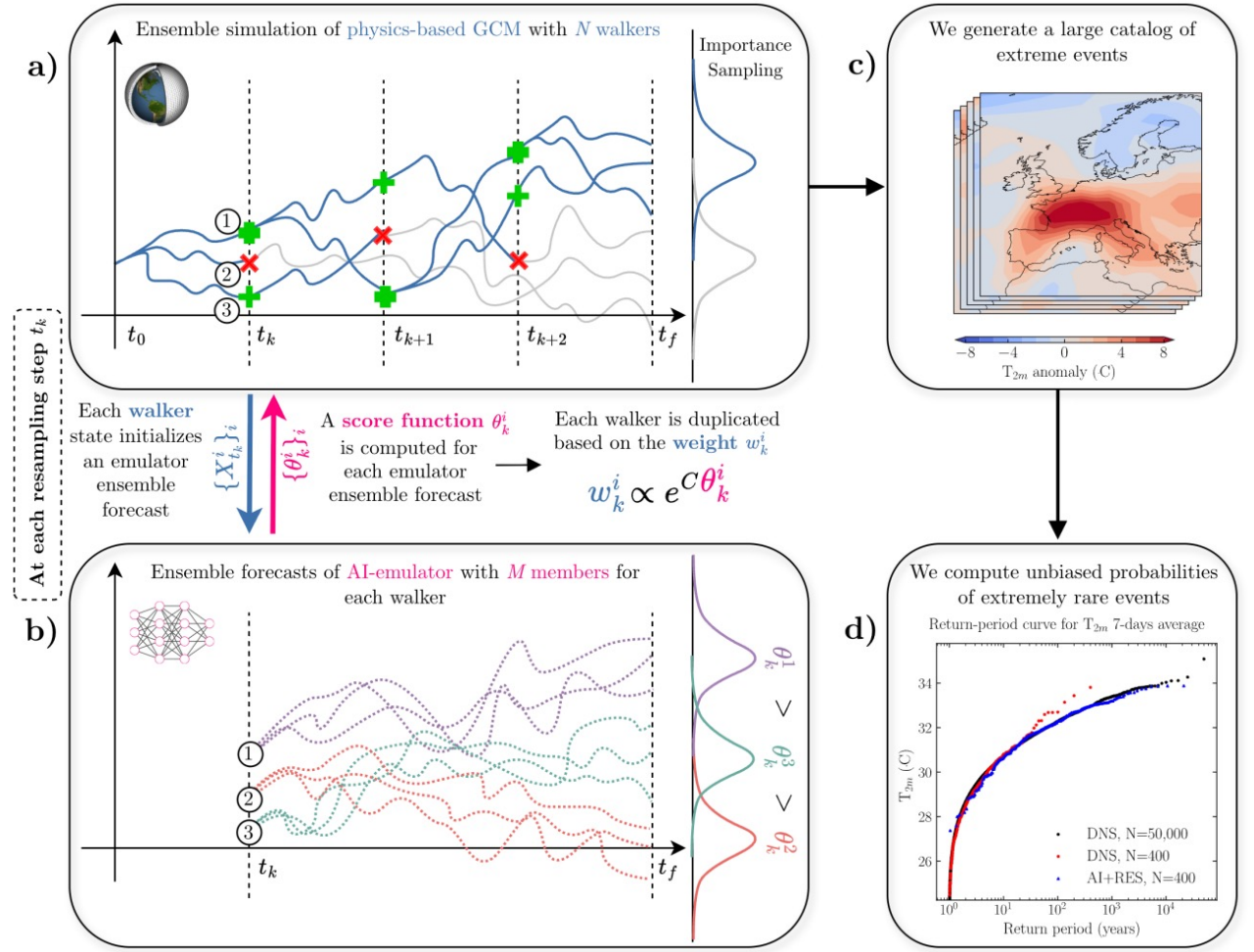
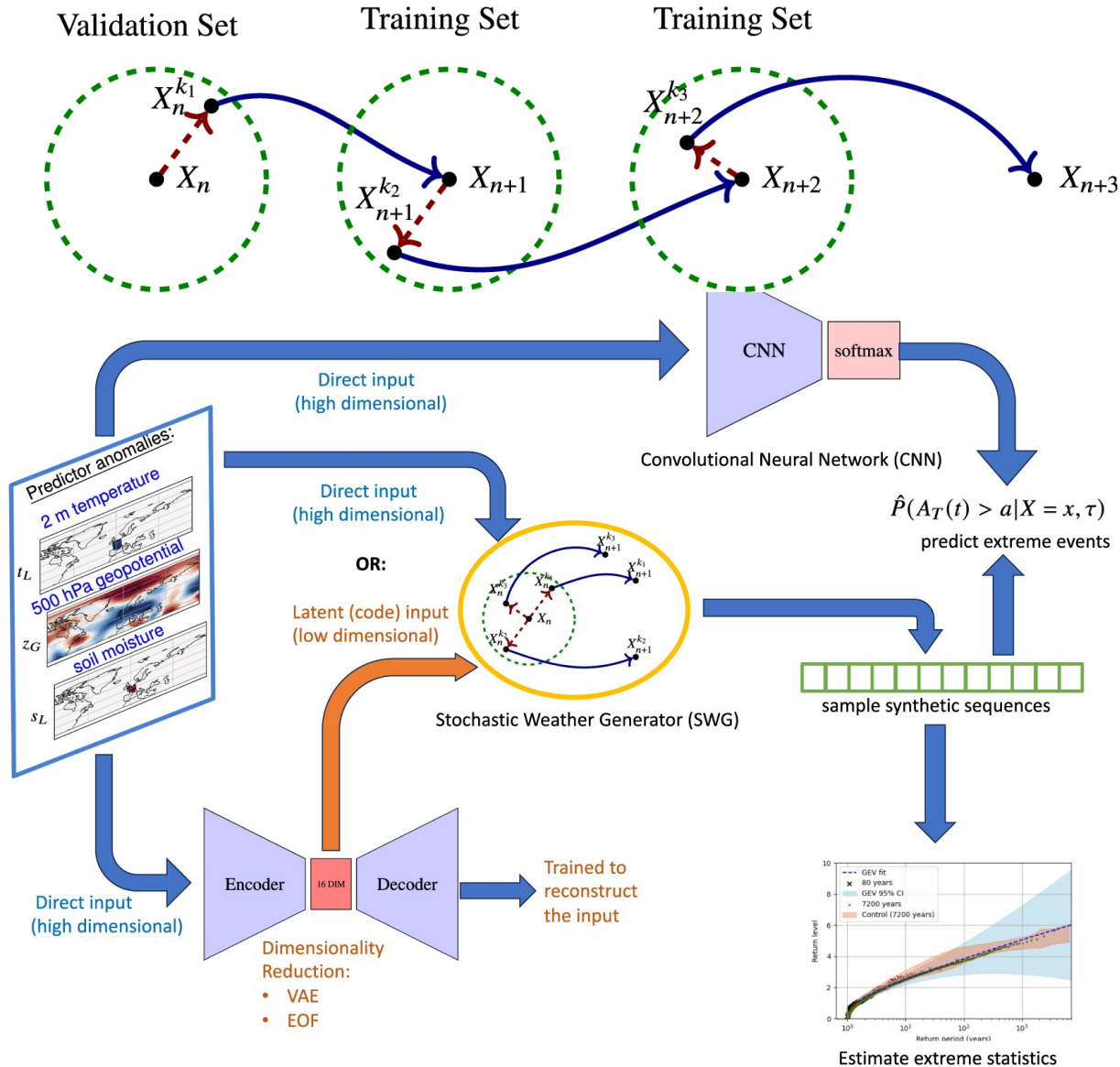
$$\frac{\partial f_s}{\partial t} + \mathbf{v} \cdot \frac{\partial f_s}{\partial \mathbf{x}} + \frac{e_s}{m_s} \left( \mathbf{E} + \frac{\mathbf{v} \times \mathbf{B}}{c} \right) \cdot \frac{\partial f_s}{\partial \mathbf{v}} = 0,$$



# Subgrid closure



# 9 Using surrogates for extreme value analysis



## Physics-informed neural networks: A deep learning framework for solving forward and inverse problems involving nonlinear partial differential equations

M Raissi, P Perdikaris, GE Karniadakis - Journal of Computational physics, 2019 - Elsevier

... We introduce **physics-informed neural networks** – **neural networks** that are trained to solve supervised learning tasks while respecting any given laws of **physics** described by general ...

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### Forward Problem:

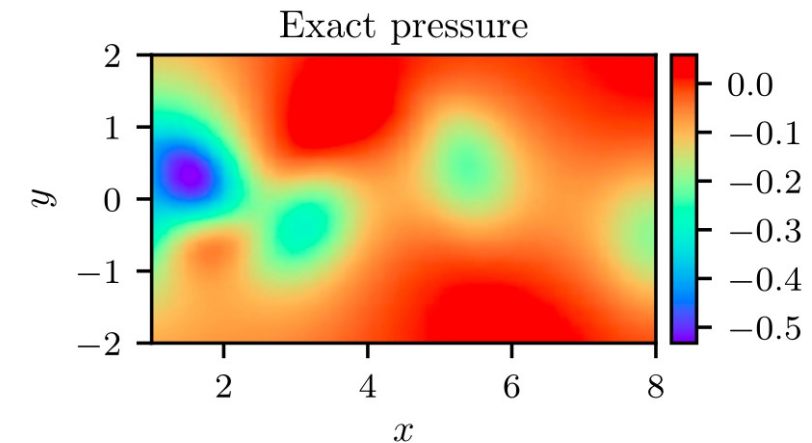
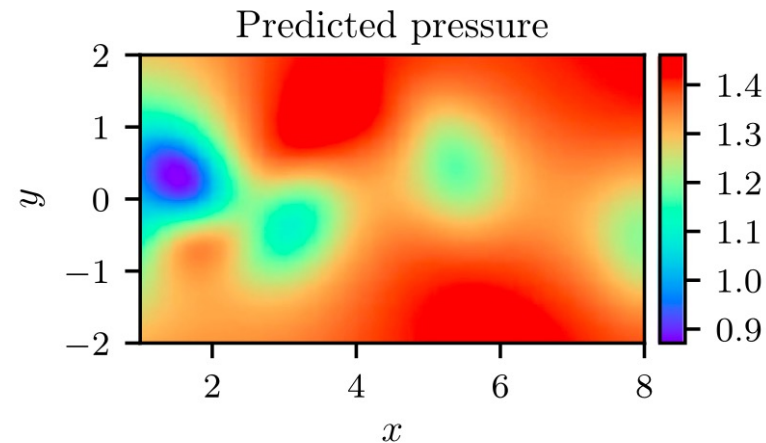
$$u_t + \mathcal{N}[u] = 0, \quad x \in \Omega, \quad t \in [0, T]$$

$$MSE = MSE_u + MSE_f$$

$$MSE_u = \frac{1}{N_u} \sum_{i=1}^{N_u} |u(t_u^i, x_u^i) - u^i|^2,$$

$$MSE_f = \frac{1}{N_f} \sum_{i=1}^{N_f} |f(t_f^i, x_f^i)|^2.$$

### Inverse Problem:

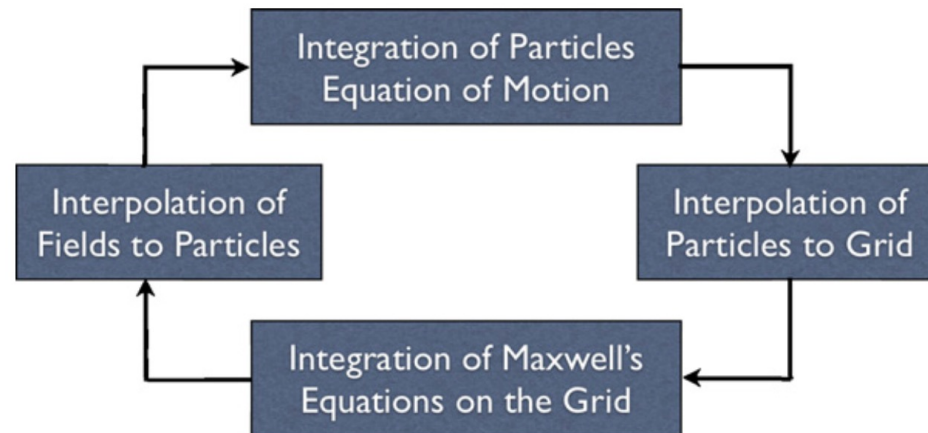
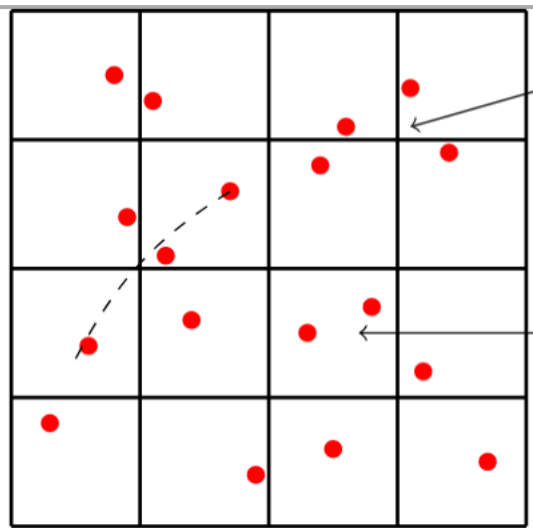


Correct PDE	$u_t + (uu_x + vv_y) = -p_x + 0.01(u_{xx} + u_{yy})$ $v_t + (uv_x + vv_y) = -p_y + 0.01(v_{xx} + v_{yy})$
Identified PDE (clean data)	$u_t + 0.999(uu_x + vv_y) = -p_x + 0.01047(u_{xx} + u_{yy})$ $v_t + 0.999(uv_x + vv_y) = -p_y + 0.01047(v_{xx} + v_{yy})$
Identified PDE (1% noise)	$u_t + 0.998(uu_x + vv_y) = -p_x + 0.01057(u_{xx} + u_{yy})$ $v_t + 0.998(uv_x + vv_y) = -p_y + 0.01057(v_{xx} + v_{yy})$

# The model hierarchy in collisionless plasmas

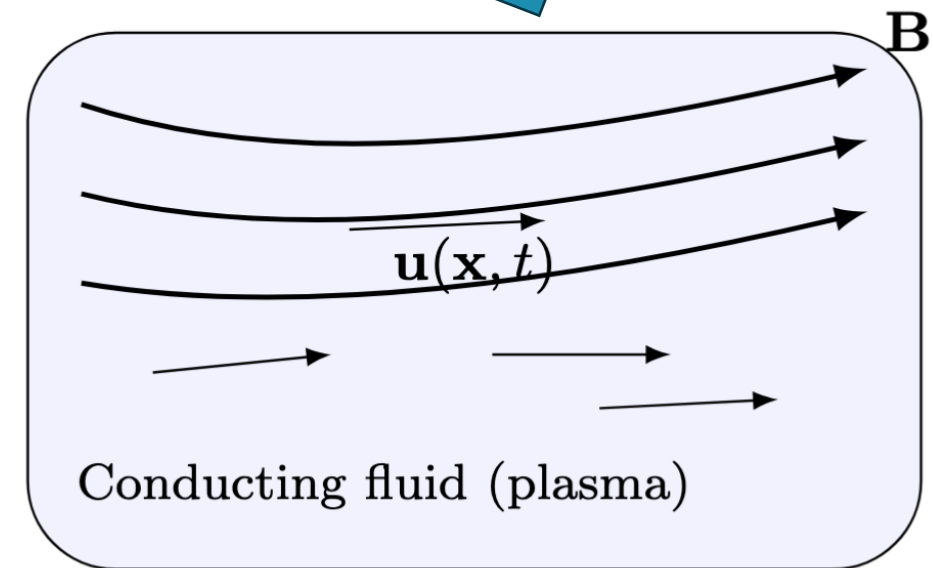
- Kinetic Modelling, Particle in Cell (PIC)

$$\frac{\partial f_s}{\partial t} + \mathbf{v} \cdot \frac{\partial f_s}{\partial \mathbf{x}} + \frac{e_s}{m_s} \left( \mathbf{E} + \frac{\mathbf{v} \times \mathbf{B}}{c} \right) \cdot \frac{\partial f_s}{\partial \mathbf{v}} = 0,$$



- MHD (fluid modelling)

$$\rho \left[ \frac{\partial \mathbf{V}}{\partial t} + (\mathbf{V} \nabla) \mathbf{V} \right] = -\nabla P + \mathbf{j} \times \mathbf{B},$$

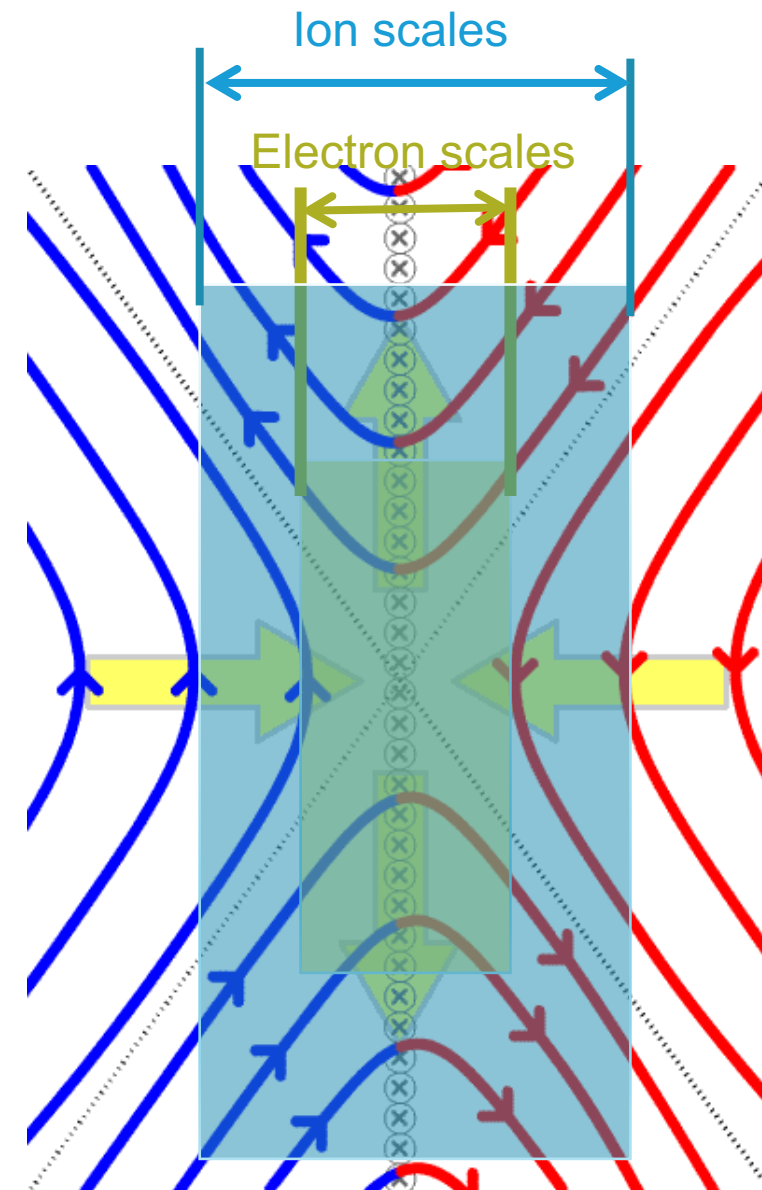
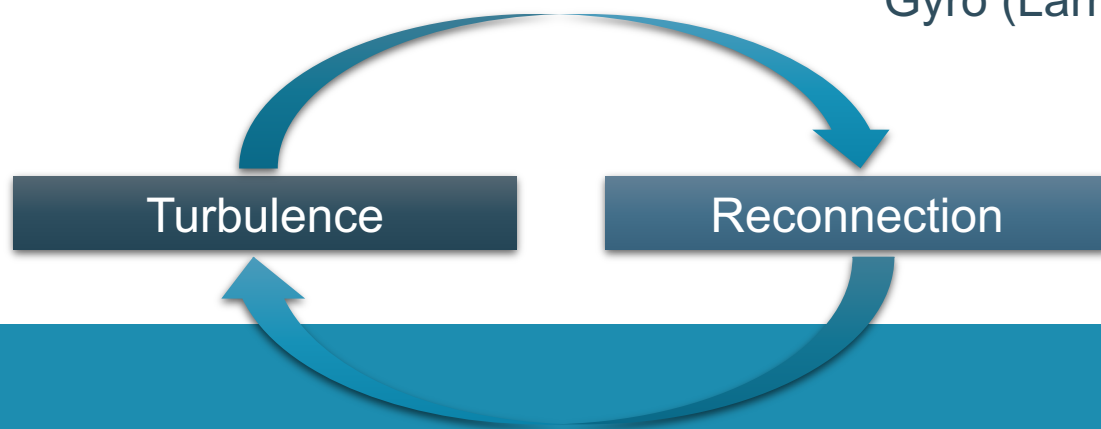
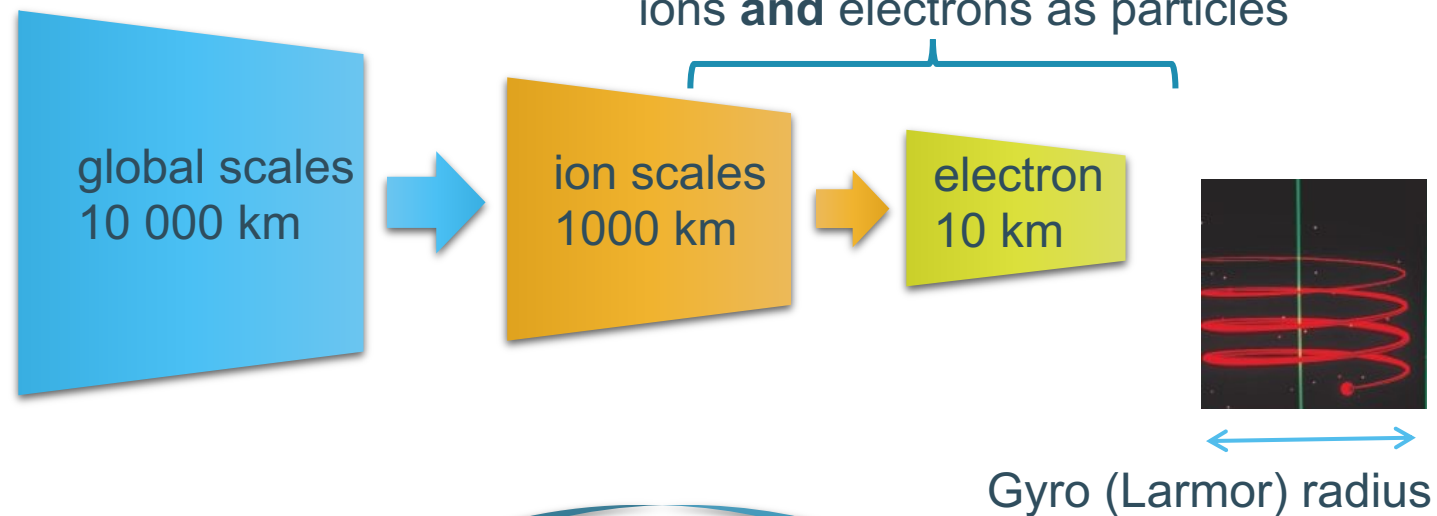


# Magnetic reconnection

Magnetohydrodynamics

ions as particles **but** electrons fluid

ions **and** electrons as particles



# VSWMC models (operational (17) and **operational soon (5)**)



## **Solar corona models:**

- Multi-VP
- Wind-Predict
- EUHFORIA-corona (WSA)
- **COCONUT**
- **COCONUT-TDm/RBSL**

## **Inner heliosphere wind and CME evolution models :**

- EUHFORIA
- **ICARUS**

## **SEP models :**

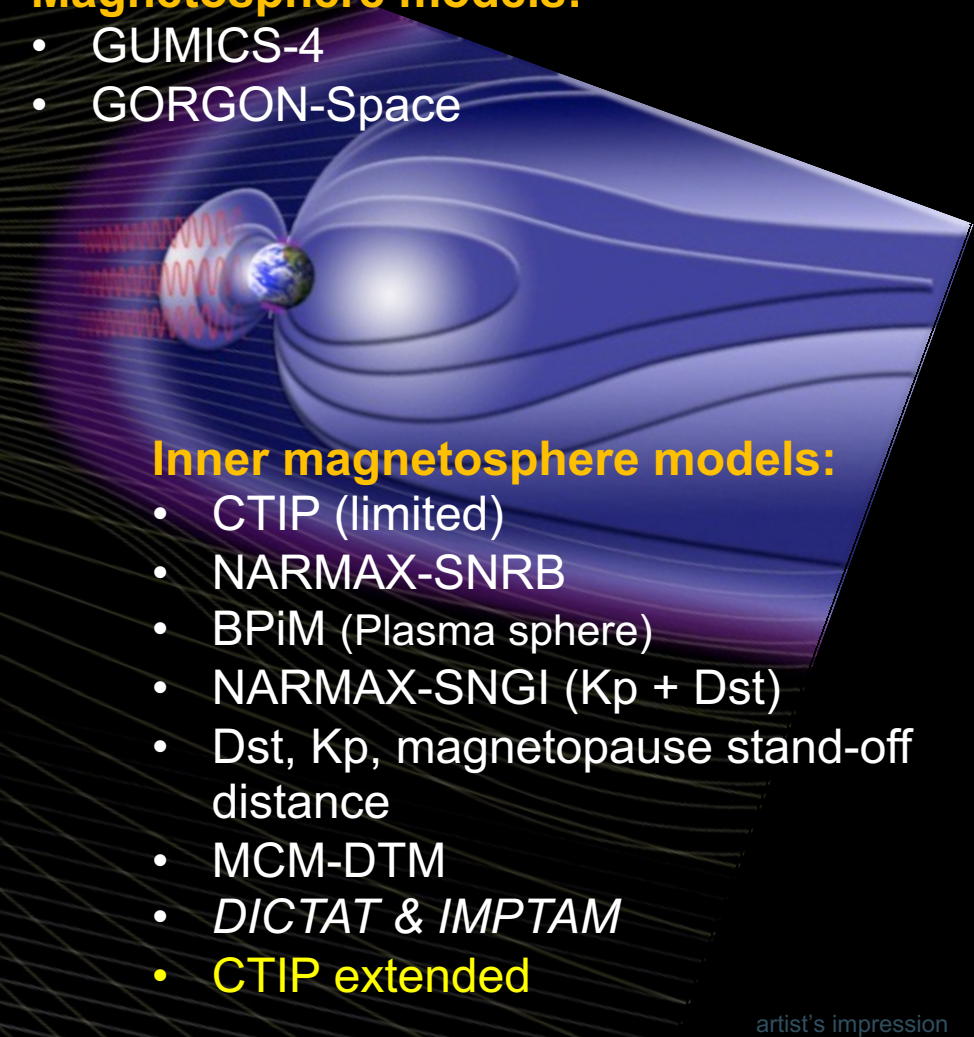
- SPARX
- **PARADISE (/ PARASOL?)**

## **Magnetosphere models:**

- GUMICS-4
- GORGON-Space

## **Inner magnetosphere models:**

- CTIP (limited)
- NARMAX-SNRB
- BPiM (Plasma sphere)
- NARMAX-SNGI (Kp + Dst)
- Dst, Kp, magnetopause stand-off distance
- MCM-DTM
- *DICTAT & IMPTAM*
- **CTIP extended**

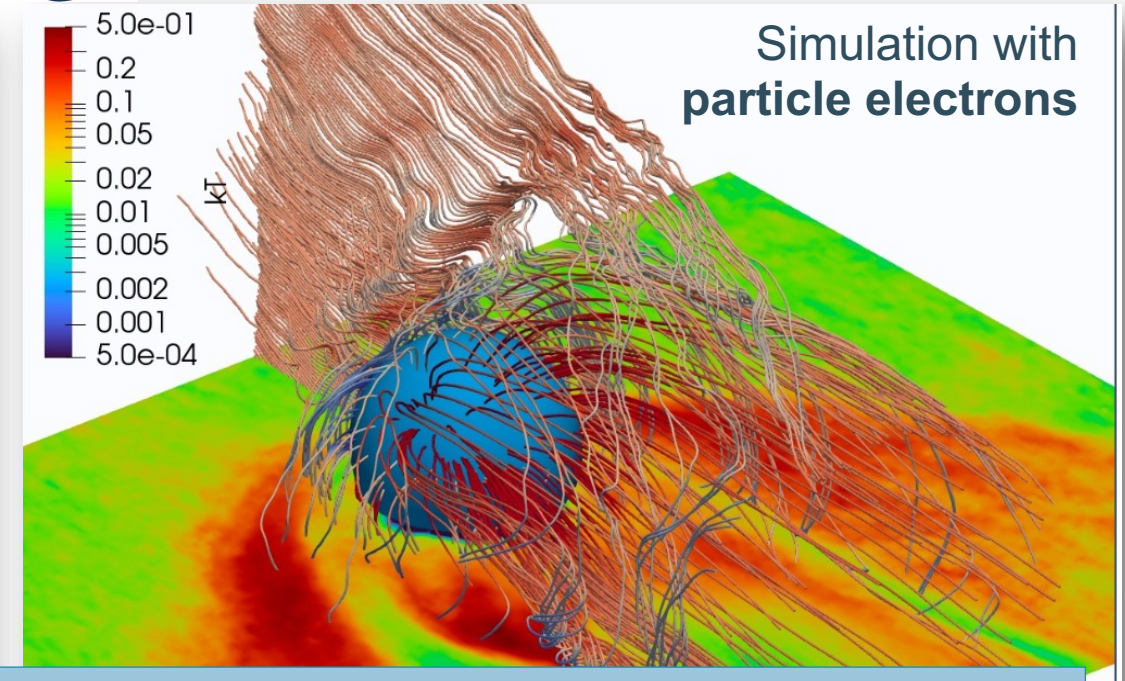
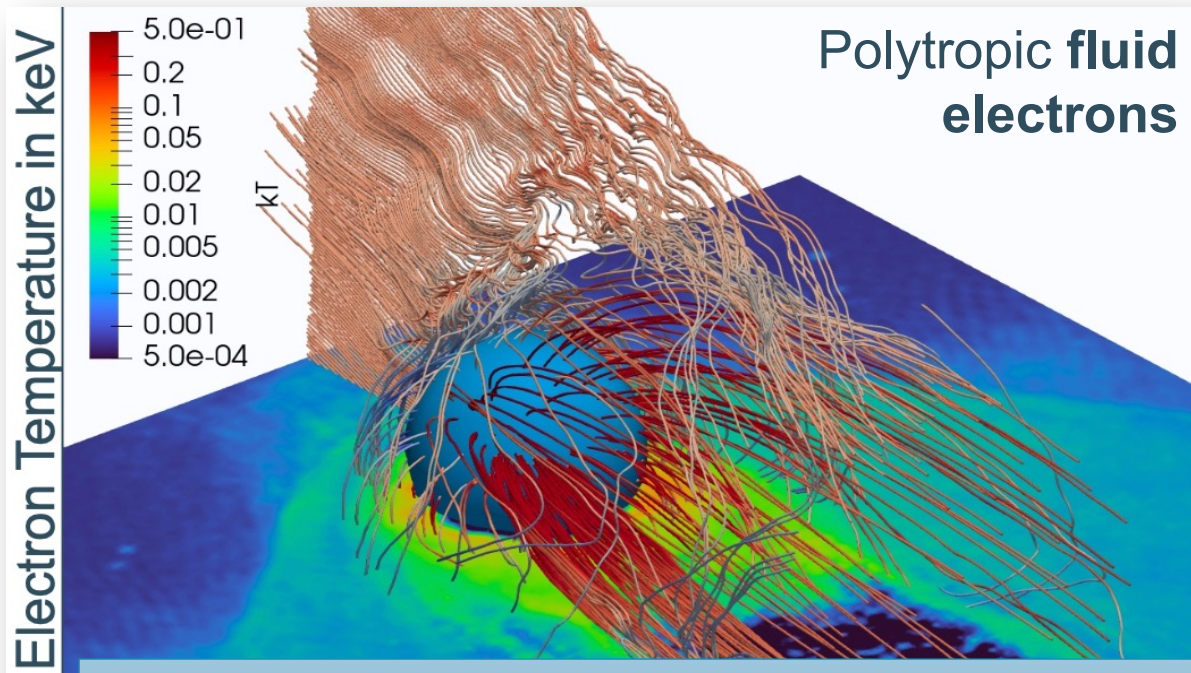


# Problem: How are particles energized in magnetospheres?



Giovanni Lapenta

ECsim = Energy Conserving PIC



Problem: modelling self-consistently **single Earth sub-storm** with electrons as particles would require **> 10 billion CPU hours!**



# From kinetic to fluid: moment closure problem

Conservation of mass:

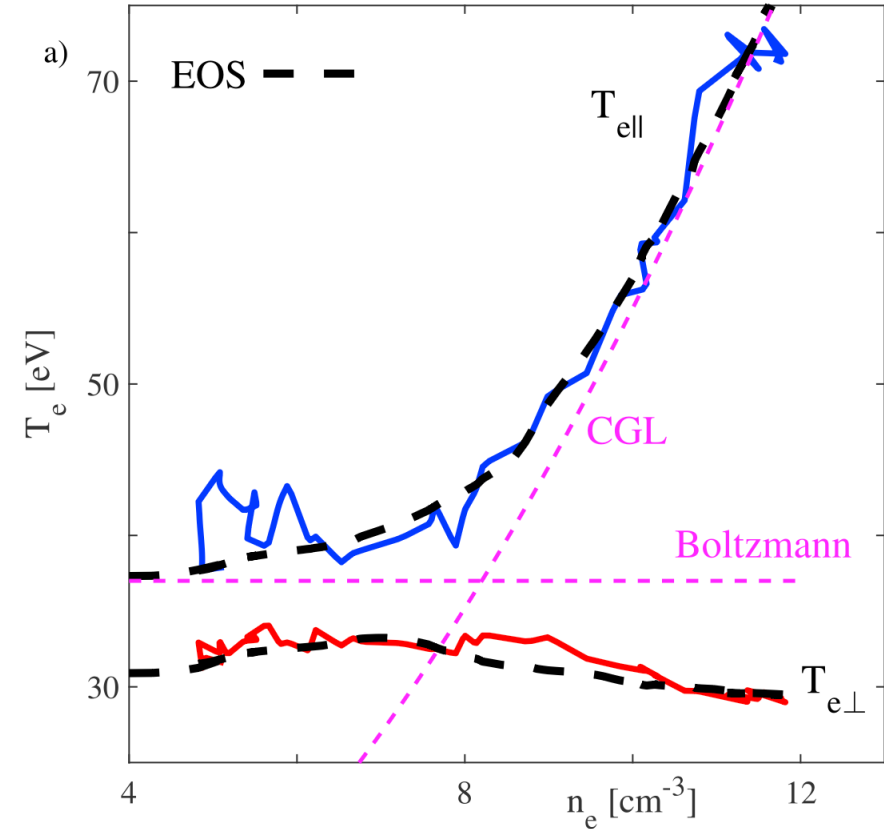
$$\frac{\partial \rho_s}{\partial t} + \nabla \cdot (\rho_s \mathbf{V}_s) = 0$$

Conservation of momentum:

$$\rho_s \left( \frac{\partial \mathbf{V}_s}{\partial t} + (\mathbf{V}_s \cdot \nabla) \mathbf{V}_s \right) = -\nabla \cdot \mathbf{P}_s + n_s q_s (\mathbf{E} + \mathbf{V}_s \times \mathbf{B})$$

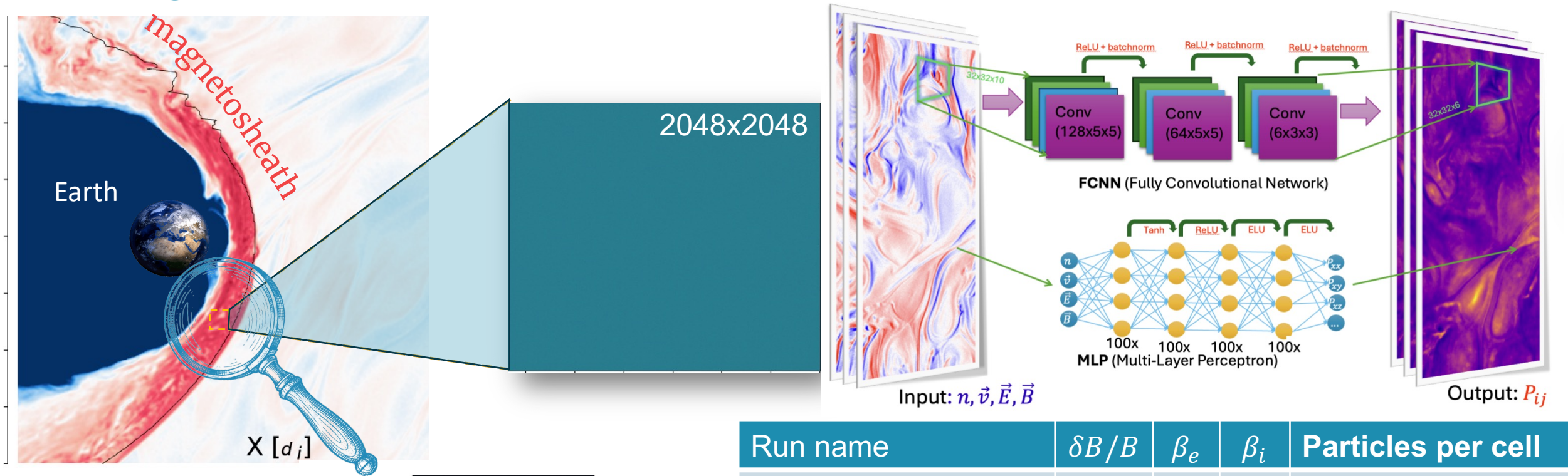
$$\mathbf{P}_s = m_s \int (\mathbf{v} - \mathbf{V})(\mathbf{v} - \mathbf{V}) f_s d\mathbf{v};$$

$$\mathbf{Q}_s = m_s \int (\mathbf{v} - \mathbf{V})(\mathbf{v} - \mathbf{V})(\mathbf{v} - \mathbf{V}) f_s d\mathbf{v}.$$

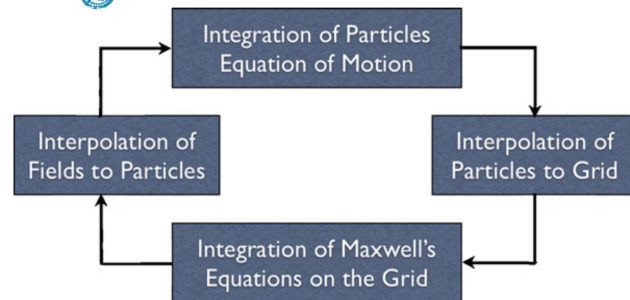


Empirical evidence for pressure equation of state in-situ

# Magnetosheath simulation of 2D decaying turbulence

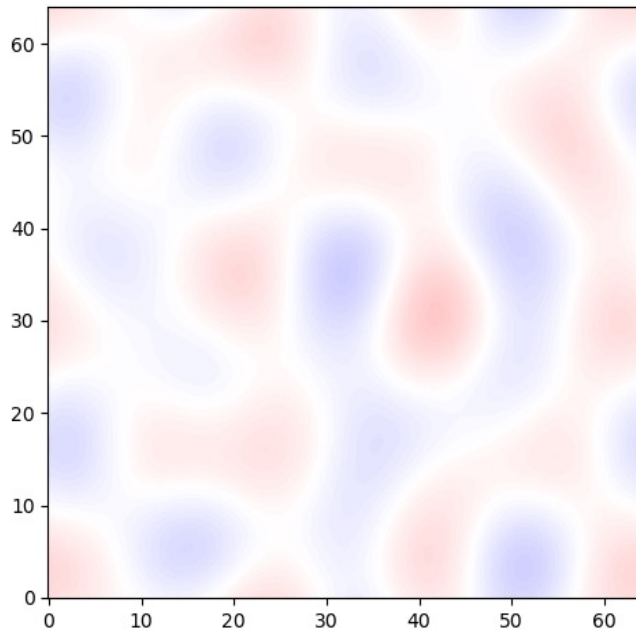


ECsim – Energy conserving, semi-implicit particle in cell code (fully kinetic)



Run name	$\delta B/B$	$\beta_e$	$\beta_i$	Particles per cell
1 (generalization)	0.5	2	8	5000
4 (training)	0.5	2	8	256
1 (validation)	0.5	2	8	256
1 (testing)	0.5	2	8	256

# Hybrid PIC (Menura) with electron closure



Fully Kinetic PIC

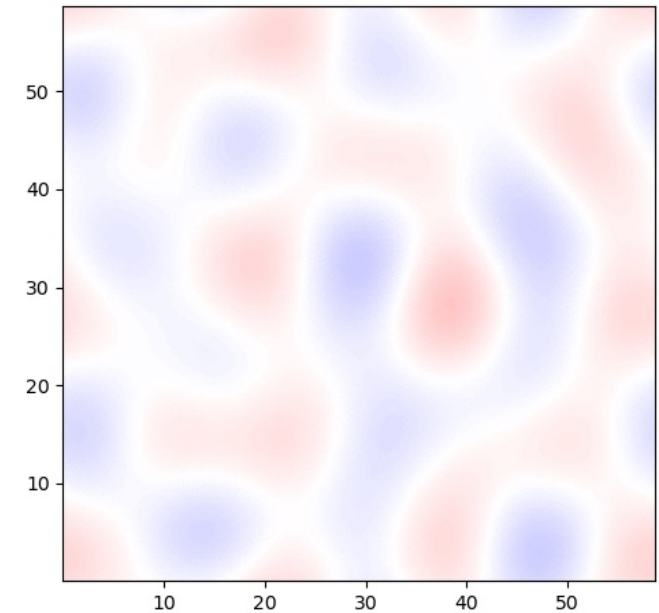
Computation time: **3 days on 128 nodes**

$$\mathbf{P} = \mathbf{P}_{NN}(n_e, \mathbf{v}_e, \mathbf{B})$$

$$\mathbf{P} \rightarrow \mathcal{G}^3 \nabla \cdot \mathbf{P}$$

$$\mathbf{B} \rightarrow \mathcal{G}^1 \mathbf{B}$$

$$\mathbf{E} \rightarrow \mathcal{G}^1 \mathbf{E}$$

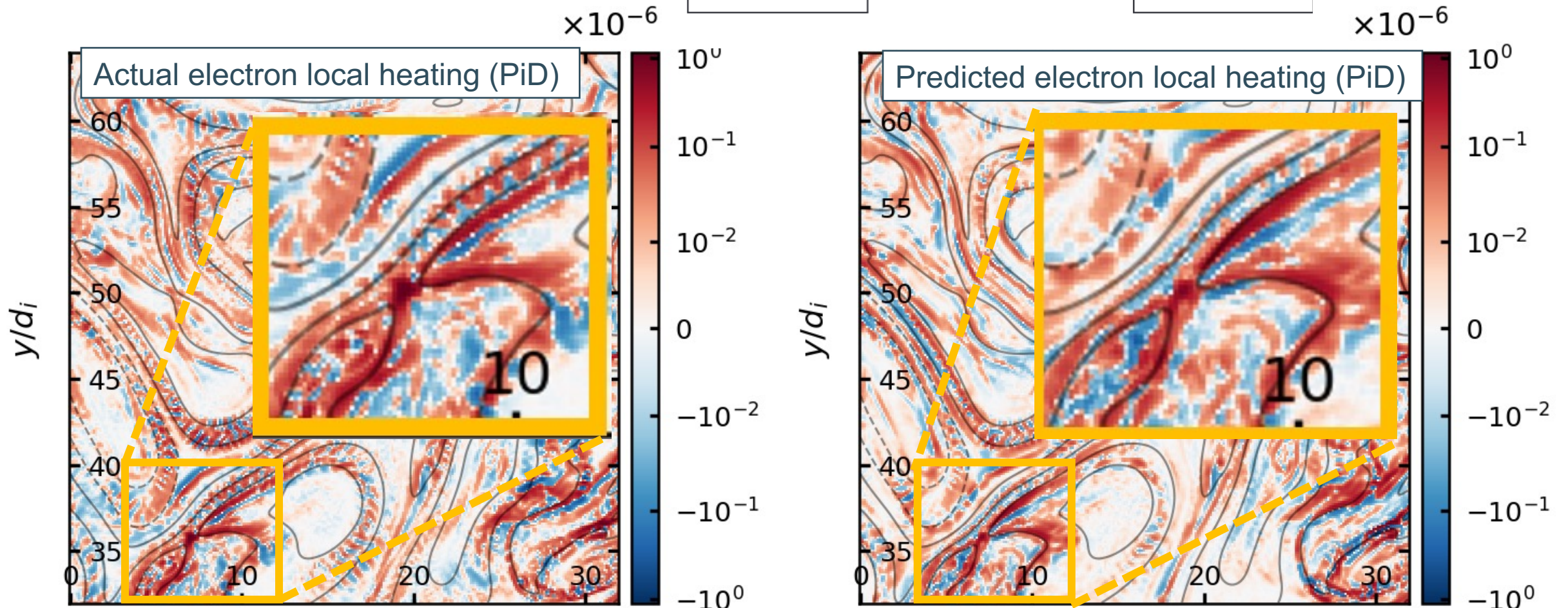
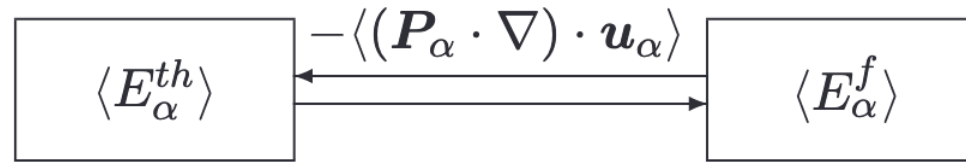


Hybrid PIC with neural closure

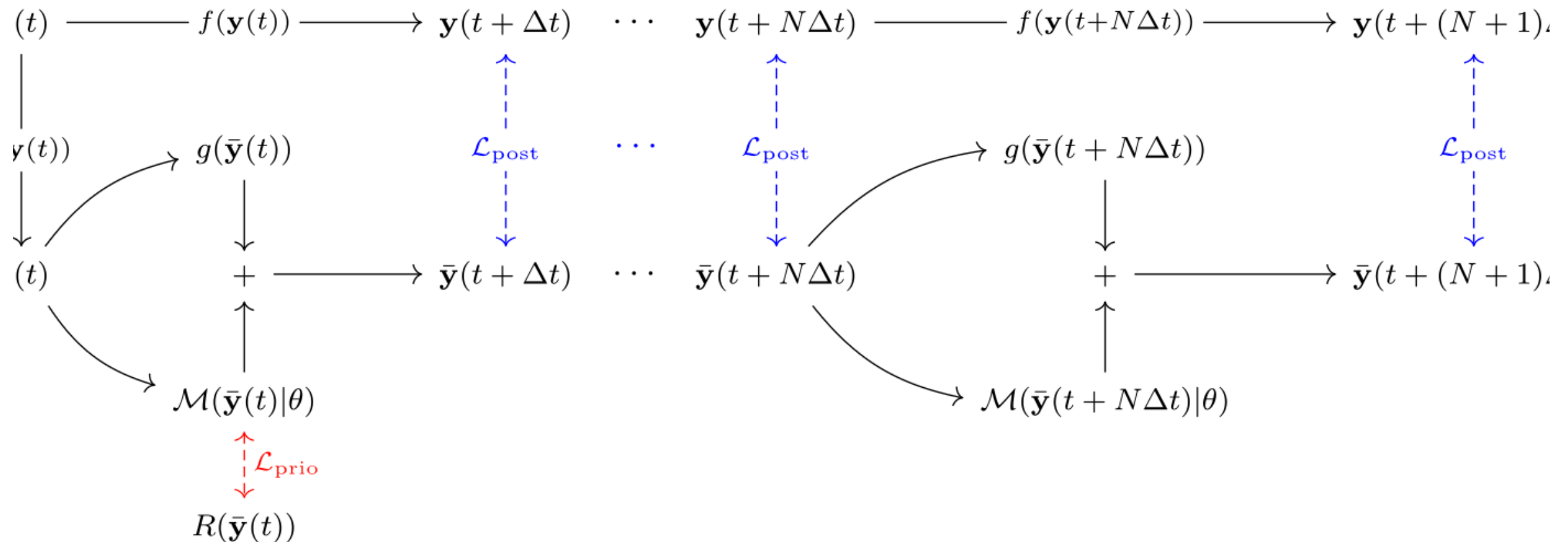
Computation time: **30 minutes on 1 node**

# Generalization to 5000 particles/cell

PiD: Incompressible pressure-strain:

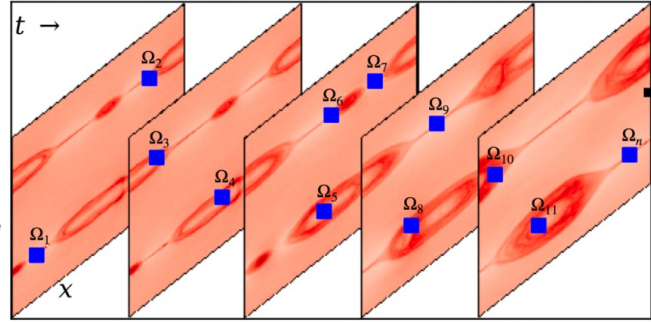


# Online stability: Online training

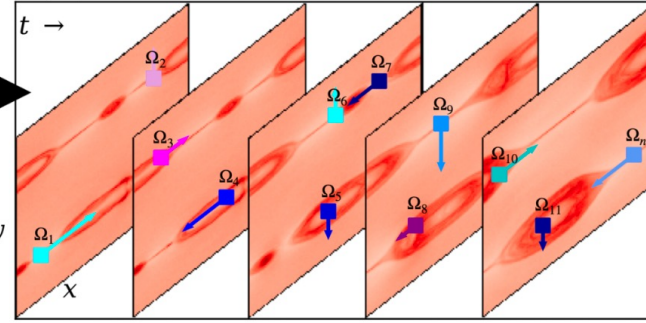


# Interpretability: Symbolic and Sparse regression

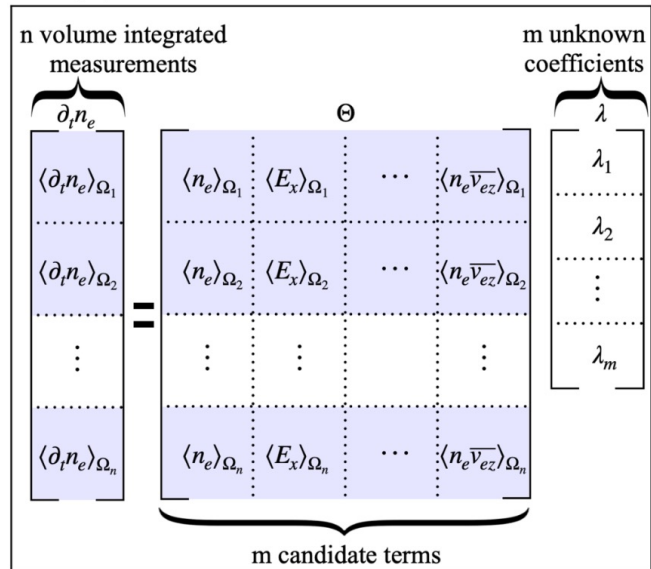
(a1) Randomly sample PIC simulation data (lab-frame data)



(b1) Lorentz boost lab-frame data in random directions



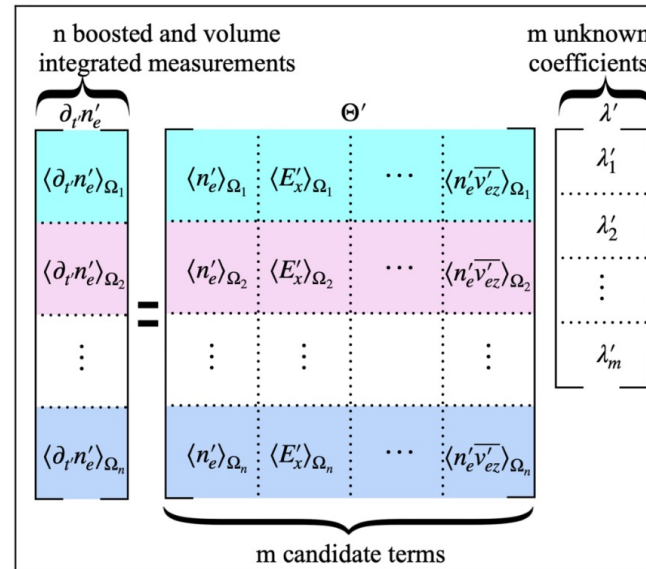
(a2) Construct candidate terms with lab-frame data



(a3) Solve sparse regression with lab-frame data

$$\min_{\lambda} ||\partial_t n_e - \Theta \lambda||_2^2 + \xi ||\lambda||_0$$

(b2) Construct candidate terms with Lorentz-boosted data



(b3) Solve sparse regression with Lorentz-boosted data

$$\min_{\lambda'} ||\partial_t n'_e - \Theta' \lambda'||_2^2 + \xi ||\lambda'||_0$$

Identified in Lab frame:

$$P_{e||\text{Lab}} = -0.069 + 0.113n_e + 0.370\overline{v_{ex}}^2 - 0.291\overline{v_{ez}}^2 - 0.078B_x^2 + 0.065B_z^2 - 0.075B_z n_e.$$

Identified with Galilean boost augmentations

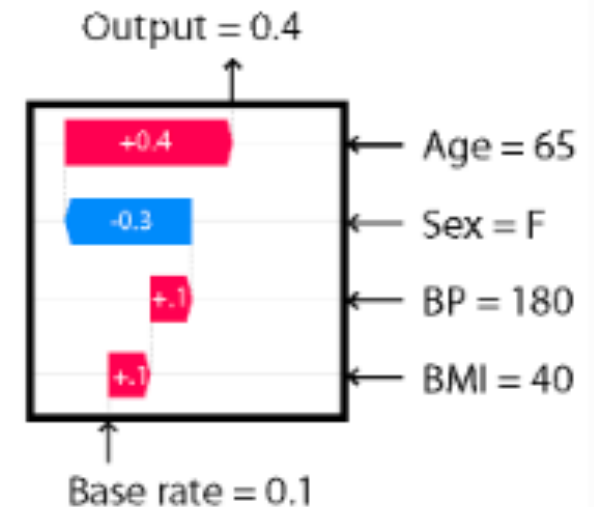
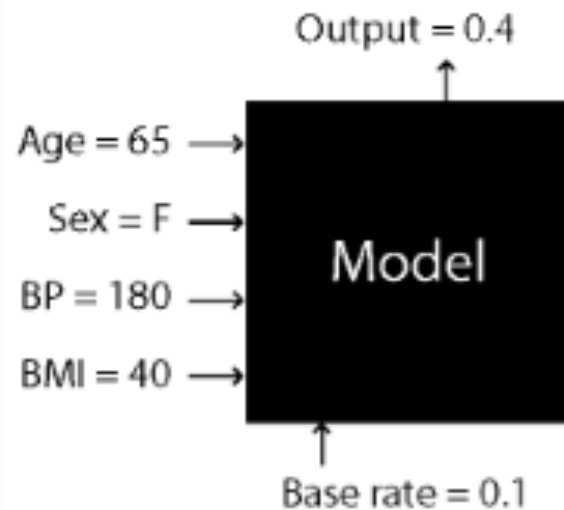
$$P_{e||\text{Boost}} = -0.071 + 0.103n_e - 0.040B_x^2 + 0.193B_y^2 + 0.062B_z^2 - 0.062B_z n_e$$

# Main limitations: when to be careful

- Poor quality of data
- Out-of-distribution (OOD)
- Rare events
- Interpretability vs Explainability



SHAP



# Use cases for AI in simulations:

- Detection of events
- Forecasting outcome
- Surrogate modelling
- Checkpoint management
- Data-driven discovery
- Subgrid closure



Fall 2026:  **D-SURGE**

Data-driven Simulations for Understanding Reconnection in GEomagnetism